

<p>Vector equation of a line with cross product</p>	$(\mathbf{r} - \mathbf{a}) \times \mathbf{b} = \mathbf{0}$ <p>where \mathbf{a} is the position vector of a point the line passes through \mathbf{b} is the direction vector</p>
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<p>Shortest distance between skew lines</p> $l_1 : \mathbf{r} = \mathbf{a} + \lambda \mathbf{b}$ $l_2 : \mathbf{r} = \mathbf{c} + \mu \mathbf{d}$	$\left \frac{(\mathbf{a} - \mathbf{c}) \cdot (\mathbf{b} \times \mathbf{d})}{ \mathbf{b} \times \mathbf{d} } \right $
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Area of a triangle	$\frac{1}{2} \mathbf{a} \times \mathbf{b} $
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Area of a parallelogram	$ \mathbf{a} \times \mathbf{b} $
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Volume of a Parallelepiped	$ \mathbf{a} \cdot \mathbf{b} \times \mathbf{c} $
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Volume of a Tetrahedron	$\frac{1}{6} \mathbf{a} \cdot \mathbf{b} \times \mathbf{c} $
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t -formula for $\sin \theta$
where $t = \tan \frac{\theta}{2}$

$$\sin \theta = \frac{2t}{1+t^2}$$

t -formula for $\cos \theta$
where $t = \tan \frac{\theta}{2}$

$$\cos \theta = \frac{1-t^2}{1+t^2}$$

t -formula for $\tan \theta$
where $t = \tan \frac{\theta}{2}$

$$\tan \theta = \frac{2t}{1 - t^2}$$

t -formula for $\frac{dt}{d\theta}$
(Weierstrass substitution)
where $t = \tan \frac{\theta}{2}$

$$\frac{dt}{d\theta} = \frac{1}{2}(1 + t^2)$$

<p>Simpson's rule for</p> $\int_a^b y \, dx$	$\approx \frac{1}{3}h\{(y_0 + y_{2n})$ $+ 4(y_1 + \dots + y_{2n-1})$ $+ 2(y_2 + \dots + y_{2n-2})\}$ <p>where $h = \frac{b-a}{2n}$</p>
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<p>Taylor series powers of x</p>	$f(x + a) = \sum_{n=0}^{\infty} \frac{f^{(n)}(a)x^n}{n!}$
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<p>Leibnitz's formula for</p> $\frac{d^n y}{dx^n}$	$\frac{d^n y}{dx^n} = \sum_{k=0}^n \binom{n}{k} \frac{d^k u}{dx^k} \frac{d^{(n-k)} u}{dx^{(n-k)}}$
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<p>3×3 matrix for reflection in the plane $x = 0$</p>	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$
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3×3 matrix for reflection in the plane $y = 0$

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

3×3 matrix for reflection in the plane $z = 0$

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$$

3×3 matrix for rotation about the x -axis

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta & -\sin \theta \\ 0 & \sin \theta & \cos \theta \end{pmatrix}$$

3×3 matrix for rotation about the y -axis

$$\begin{pmatrix} \cos \theta & 0 & \sin \theta \\ 0 & 1 & 0 \\ -\sin \theta & 0 & \cos \theta \end{pmatrix}$$

<p>3×3 matrix for rotation about the z-axis</p>	$\begin{pmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{pmatrix}$
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<p>Complex loci $z - a = b$</p>	<p>Circle centre a, radius b</p>
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Complex loci $ z - a = z - b $	Perpendicular bisector of the line joining the complex numbers a and b
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Complex loci $\arg(z - a) = \beta$	Half line from the complex number a at an angle of β to the real axis
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<p>Direction cosines of the line $\mathbf{r} = \mathbf{a} + \lambda \mathbf{b}$, where $\mathbf{b} = \begin{pmatrix} x \\ y \\ z \end{pmatrix}$</p>	<p>The angle that the line makes with the axes. Angle with the x-axis, α $\cos \alpha = \frac{x}{ b }$ Angle with the y-axis, β $\cos \beta = \frac{y}{ b }$ Angle with the z-axis, γ $\cos \gamma = \frac{z}{ b }$</p>
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<p>Polar graph $r = p \sec(\alpha - \theta)$</p>	<p>Straight line Convert into $y = mx + c$ using the addition formula for cosine</p>
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Polar graph $r = a$	Circle centre the pole, radius a
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Polar graph $r = 2a \cos \theta$	Circle centre $(a, 0)$, radius a One symmetric petal
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Polar graph $r = \theta$	Spiral centred at origin
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Polar graph $r = a \cos n\theta$	Only considering $r \geq 0$ Rose with n petals spaced at $\frac{2\pi}{n}$ starting at $(a, 0)$
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<p>Polar graph $r = p + q \cos \theta$ $q \leq p < 2q$</p>	<p>Concave curve “dimple” shaped limaçon</p>
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<p>Polar graph $r = p + q \cos \theta$ $p = q$</p>	<p>Cardioid</p>
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<p>Polar graph $r = p + q \cos \theta$ $p \geq 2q$</p>	<p>Convex curve “egg” shaped limaçon</p>
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<p>Polar graph $r^2 = a^2 \cos 2\theta$</p>	<p>Lemiscate (figure-8 shaped) starting at $(a, 0)$</p>
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