

Jamie has 80 beads in blue and green in a ratio 5 : 3

They are then given additional beads.

They are given the same number of both colours and now have a ratio 13 : 9

How many beads were they given?

<i>B : G</i>	Total	
5 : 3	8) × 10
50 : 30	80	

Before		After		
<i>B : G</i>	Diff	<i>B : G</i>	Diff	
50 : 30	20	13 : 9	4) × 5
			20	

Jamie has blue to green beads in a ratio 5 : 2

They exchange some blue beads for the same number of green beads.

The ratio of beads is now 4 : 5

What is the smallest number of beads they could have started with?

How many beads did they exchange?

Before		After	
<i>B : G</i>	Total	<i>B : G</i>	Total
5 : 2	7	4 : 5	9

Jamie has 90 beads in blue and green in the ratio 3 : 7

They gave away the same number of each bead.

Now they have beads in the ratio 1 : 7

How many beads do they have at the end?

$B : G$	Total
3 : 7	
:	90

Before		After	
$B : G$	Diff	$B : G$	Diff
		1 : 7	6

Jamie and Tyler have beads in a ratio of 4 : 5

Jamie gives some of their beads to Tyler.

The ratio is now 3 : 7

Find the smallest number of beads they could have started with
and how many beads Jamie gives to Tyler.

The following ratios are equivalent

$$x - 1 : x + 1 \text{ and } x + 3 : x + 7$$

Find x

$$\begin{array}{r} x - 1 : x + 1 \\ x + 3 : x + 7 \end{array} \begin{array}{r} \text{Diff} \\ 2 \\ 4 \end{array} \begin{array}{l} \curvearrowright \\ \times 2 \end{array}$$

$$2(x - 1) = x + 3$$

The following ratios are equivalent

$$14 - x : 4 + x \text{ and } 20 - 3x : 1 + 3x$$

Find x

$$\begin{array}{r} 14 - x : 4 + x \\ 20 - 3x : 1 + 3x \end{array} \begin{array}{r} \text{Total} \\ 18 \\ 21 \end{array} \begin{array}{l} \curvearrowright \end{array}$$

The following ratios are equivalent

$$14 + x : 19 + x \text{ and } 24 + 3x : 30 + 3x$$

Find x

Jamie has 80 beads in blue and green in a ratio 5 : 3

They are then given additional beads.

They are given the same number of both colours and now have a ratio 13 : 9

How many beads were they given?

$B : G$	Total	
5 : 3	8) $\times 10$
50 : 30	80	

Before		After	
$B : G$	Diff	$B : G$	Diff
50 : 30	20	13 : 9	4
		<u>65 : 45</u>	20

) $\times 5$

15 of each colour

Jamie has blue to green beads in a ratio 5 : 2

They exchange some blue beads for the same number of green beads.

The ratio of beads is now 4 : 5

What is the smallest number of beads they could have started with?

How many beads did they exchange?

LCM of total	Before		After	
	$B : G$	Total	$B : G$	Total
$\times 9$ (5 : 2	7	4 : 5	9
	<u>45 : 18</u>	<u>63</u>	<u>28 : 35</u>	<u>63</u>

) $\times 7$

Exchanged 27 beads

Jamie has 90 beads in blue and green in the ratio 3 : 7

They gave away the same number of each bead.

Now they have beads in the ratio 1 : 7

How many beads do they have at the end?

$$\begin{array}{l} B : G \quad \text{Total} \\ 3 : 7 \quad 10 \\ 27 : 63 \quad 90 \end{array} \downarrow \times 9$$

Before		After	
B : G	Diff	B : G	Diff
27 : 63	36	1 : 7	6
		6 : 42	36

$$\downarrow \times 6$$

48 beads at the end.

Jamie and Tyler have beads in a ratio of 4 : 5

Jamie gives some of their beads to Tyler.

The ratio is now 3 : 7

Find the smallest number of beads they could have started with
and how many beads Jamie gives to Tyler.

Before		After	
B : T	Total	B : T	Total
4 : 5	9	3 : 7	10
40 : 50	90	27 : 63	90

$$\times 10 \quad \downarrow \times 9$$

90 beads

13 beads given to Tyler

The following ratios are equivalent

$$14 + x : 19 + x \text{ and } 24 + 3x : 30 + 3x$$

Find x

$$\begin{array}{l} 14+x : 19+x \quad \frac{\text{Diff}}{5} \\ 24+3x : 30+3x \quad 6 \end{array} \quad \left. \vphantom{\begin{array}{l} 14+x : 19+x \\ 24+3x : 30+3x \end{array}} \right\} \times \frac{6}{5}$$

$$\frac{6}{5}(14+x) = 24+3x$$

$$6(14+x) = 5(24+3x)$$

$$84 + 6x = 120 + 15x$$

$$-36 = 9x$$

$$\underline{\underline{x = -4}}$$